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# Validation of GOCE gravity field models over Poland using the EGM2008 and GPS/levelling data

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**Abstract.** Since the mid of 2010, global geopotential models based on GOCE mission data became available. The first two releases of GGMs contained four different solutions while in the third release only two solutions have been generated. In the presented study the available GOCE-derived gravity field models were evaluated in terms of height anomalies and gravity anomalies over Poland with the use of the respective functionals calculated from the EGM2008 geopotential model as well as height anomalies at 184 stations of high precision GPS/levelling control traverse.

The fit of GOCE gravity field models with the EGM2008 in terms of height anomalies and gravity anomalies measured with a standard deviation is below 10 cm, and 3 mGal, respectively. Their fit with GPS/levelling height anomalies at the stations of GPS/levelling control traverse is at the level of 10 cm. The results obtained indicate some improvement of the consecutive releases of GOCE gravity field models.

**Keywords:** geopotential model, GOCE, EGM2008, GPS/levelling, height anomaly, gravity anomaly

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## 1. Introduction

The latest gravity field modelling dedicated satellite mission is the Gravity Field and Steady-state Ocean Circulation Explorer (GOCE) which is a core satellite mission of the European Space Agency (ESA) Living Planet Program (ESA, 1999). The major observable is the gravity gradient provided by high precision gradiometer mounted on the satellite equipped with high and drag-free system. The GOCE satellite was launched on 17 March 2009. The objective of the mission was to provide a static geoid model with an accuracy of 1–2 cm and gravity field model of 1 mGal accuracy in a spatial resolution of about 100 km (a half-wavelength) (Drinkwater et al., 2003).

In order to fulfil the objectives of the GOCE satellite mission, three different approaches were

applied to modelling the gravity field in GOCE High Level Processing Facility (HPF) (Rummel et al., 2004). They are denoted as a direct approach (DIR), a time-wise solution (TIM), and a space-wise solution (SPW). The main characteristics of those approaches can be described shortly as follows (Pail et al., 2011):

In direct approach, the a priori global geopotential model (GGM) EIGEN-5C (Förste et al., 2008) has been applied. The spherical harmonic coefficients and their derivatives were calculated by solving the inverse problem with the use of least squares method.

The time-wise approach is a pure solution, with no a priori gravity field information involved in the calculation. The spherical harmonic coefficients and their derivatives have been computed by solving normal equations with the use of least squares method.

In space-wise approach, the GOCE quick-look GGM – EGM\_QLO\_21 – has been used as prior gravity information. Other GGMs, in particular EGM2008, EIGEN-5C and ITG-GRACE2010 (Mayer-Gürr et al., 2010) were applied as reference gravity field models (for details see Migliaccio et al., 2010). The determination of the spherical harmonic coefficients and their derivatives was based on least squares collocation.

Beside the GOCE-only GGMs, combined geopotential models using GOCE and other satellite and terrestrial data have been generated under the Gravity Observation Combination (GOCO) project (Pail et al., 2010b).

The current GGMs based on GOCE solutions have been delivered in three releases. The major difference between the consecutive releases is the length of observation period determining data coverage, and the source of data used in the computations. The first release delivered in June 2010 was based on two months data (01 November 2009 to 31 December 2009). In March 2011, the second release was published. It was developed using already 8 months data: from November 2009 until June 2010. Subsequently, the third release published in November 2011, was based on 20 months data: from November 2009 to June 2011. More information on those releases can be found at <http://earth.esa.int/GOCE/>.

All geopotential models obtained from gravity field modelling dedicated space missions need validation in different parts of the Earth' globe. The results of validation of GGMs determined from CHAMP and then from GRACE mission data in different regions covering almost all continents were extensively described in literature. The GOCE GGMs of 1<sup>st</sup> release were evaluated, e.g. using truncated EGM2008 (up to degree and order 200) regional geoid and terrestrial gravity data over Norway. The obtained differences in height anomalies and gravity anomalies reached several decimetres with the standard deviation of 6–10 cm, and a few milligals, respectively (Šprlák et al., 2011). The 1<sup>st</sup> and 2<sup>nd</sup> releases of GOCE GGMs were similarly evaluated over the area of Slovakia. Standard deviations of the differences between height anomalies and gravity anomalies from GOCE models and truncated EGM2008 model were within the range of 6–21 cm, and 2–6 mGal, respectively (Janák and Pitoňák, 2011).

Area of Poland seems specifically suitable for validating GOCE-based GGMs due to its high precision quasigeoid (accuracy below 2 cm), high precision GPS/levelling traverse dedicated for validation of quasigeoid models (Krynski and Lyszkowicz, 2006, 2007; Krynski, 2007a). In addition, since high quality gravity data from Poland were provided for developing the EGM2008, the model fits very well gravity field over Poland (Krynski and Kloch, 2009).

The main purpose of this study is to validate gravity anomalies and height anomalies from the GGMs based on data from GOCE satellite mission with the use of gravity anomalies and height anomalies from the EGM2008 and high precision GPS/levelling sites over Poland as well as to assess the progress in GOCE mission products in terms of consecutive releases.

## 2. The global geopotential models investigated

Ten global geopotential models (Table 1) developed with the use of data from GOCE mission were evaluated. Eight of them, denoted by DIR1, DIR2, DIR3, TIM1, TIM2, TIM3, SPW1, and SPW2, are known in literature as GOCE-only models (see Migliaccio et al., 2011; Pail et al., 2011; Šprlák et al., 2011). The official names of GOCE GGMs at the International Centre for Global Earth Models (ICGEM) are given in Table 1. The last two GGMs: GOCO01 and GOCO02 are combined models. They are based on the combination of GOCE data with data from other missions. All those models are presently available at the web site <http://icgem.gfz-potsdam.de/ICGEM/>.

The EGM2008 global geopotential model was used as a reference model to validate the GOCE-based GGMs. This model was extensively evaluated over the area of Poland using four different GPS/levelling data sets and three quasigeoid models over Poland. The evaluation showed that, the fitting of EGM2008 height anomalies over Poland measured with a standard deviation is below 2 cm (Krynski and Kloch, 2009; Łyszkowicz, 2009).

## 3. Basic computation formulae

The global geopotential models given in Table 1 are expressed in terms of a set of fully normalized

Table 1. Global geopotential models investigate

GGM	Degree/order	Input data	GGM official name at ICGEM	Citation
DIR1	240	GOCE	GO_CONS_GCF_2_DIR_R1	Bruinsma et al., 2010
DIR2	240	GOCE	GO_CONS_GCF_2_DIR_R2	Bruinsma et al., 2010
DIR3	240	GOCE + GRACE + SLR	GO_CONS_GCF_2_DIR_R3	Bruinsma et al., 2010
TIM1	250	GOCE	GO_CONS_GCF_2_TIM_R1	Pail et al., 2010a
TIM2	224	GOCE	GO_CONS_GCF_2_TIM_R2	Pail et al., 2011
TIM3	250	GOCE	GO_CONS_GCF_2_TIM_R3	Pail et al., 2011
SPW1	210	GOCE	GO_CONS_GCF_2_SPW_R1	Migliaccio et al., 2010
SPW2	240	GOCE	GO_CONS_GCF_2_SPW_R2	Migliaccio et al., 2011
GOCO01	224	GOCE+GRACE	GOCO01	Pail et al., 2010b
GOCO02	250	GOCE+GRACE + CHAMP + SLR + satellite altimetry	GOCO02	Goiginger et al., 2011
EGM2008	2160	GRACE + terrestrial gravity + satellite altimetry + SLR	EGM2008	Pavlis et al., 2008

spherical harmonic coefficients  $\bar{C}_{nm}$  and  $\bar{S}_{nm}$  of  $n$  degree and  $m$  order. With the use of those coefficients gravity anomaly  $\Delta g_{(r,\varphi,\lambda)}$  and height anomaly  $\tilde{N}_{(r,\varphi,\lambda)}$  can be determined at arbitrary point  $(r, \varphi, \lambda)$  applying the following formulae (Torge, 1991):

$$\tilde{N}_{(r,\varphi,\lambda)} = \frac{GM}{a\gamma} \sum_{n=2}^{N_{\max}} \left(\frac{a}{r}\right)^{n+1} \sum_{m=0}^n (\bar{C}_{nm} \cos m\lambda + \bar{S}_{nm} \sin m\lambda) \bar{P}_{nm}(\sin\varphi) \quad (1)$$

$$\Delta g_{(r,\varphi,\lambda)} = \frac{GM}{a^2} \sum_{n=2}^{N_{\max}} (n-1) \left(\frac{a}{r}\right)^{n+2} \sum_{m=0}^n (\bar{C}_{nm} \cos m\lambda + \bar{S}_{nm} \sin m\lambda) \bar{P}_{nm}(\sin\varphi) \quad (2)$$

tions,  $N_{\max}$  is the maximum degree of gravity field model, and  $\gamma$  is the normal gravity on the reference ellipsoid at latitude  $\varphi$ .

#### 4. Comparison of GOCE-based gravity field models with the EGM2008

Free-air gravity anomalies and height anomalies were calculated on  $54' \times 54'$  grid over the region of Poland from the GOCE-based GGMs specified in Table 1. The grid corresponds to the expected reso-

lution of GOCE-derived GGMs. These anomalies have been compared with the respective ones computed similarly from the EGM2008. All GGMs used, including the EGM2008, were truncated to degree and order 200 ( $N_{\max} = 200$ ) which corresponds to the objective of GOCE mission in terms of its spatial resolution  $\sim 100$  km, and makes the results of comparison more reliable. Figures 1–4 and 5–8 show the differences between GOCE-based GGMs and the EGM2008 in terms of free-air gravity anomalies and height anomalies, respectively.

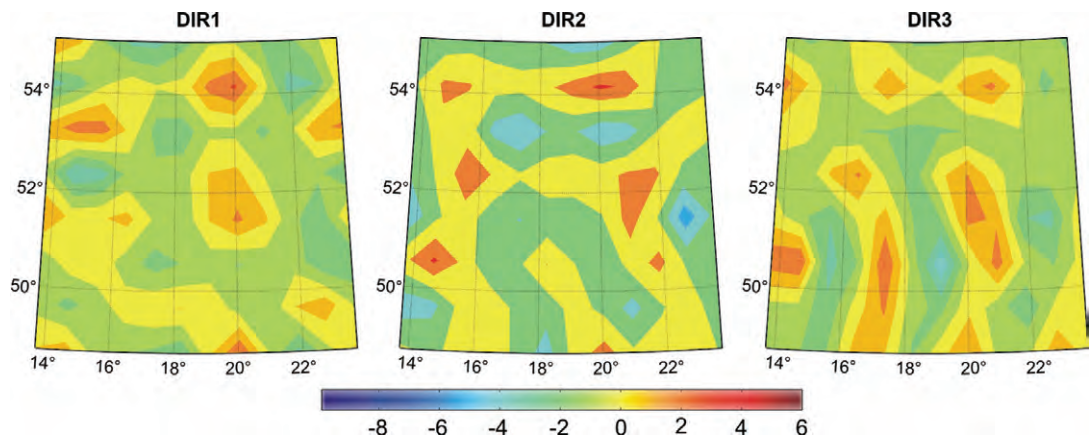


Fig. 1. Differences between free-air gravity anomalies obtained from EGM2008 and from GOCE direct solutions [mGal]

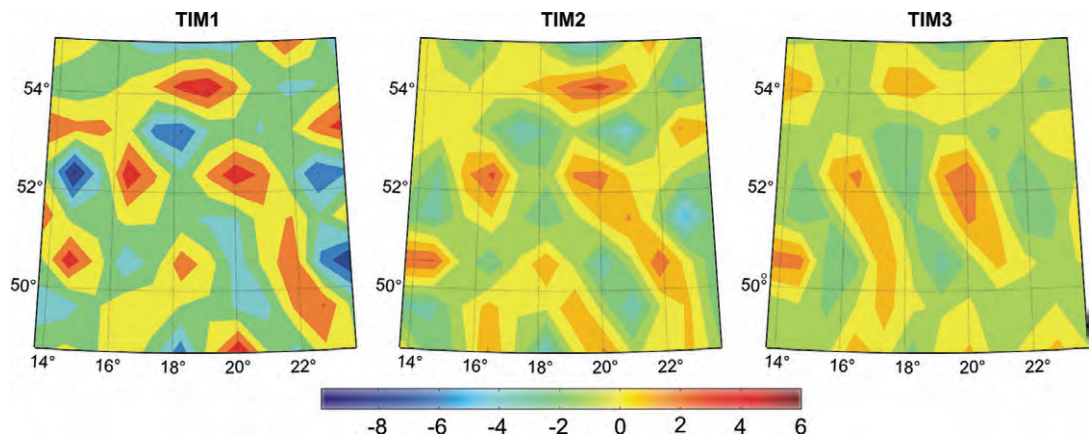


Fig. 2. Differences between free-air gravity anomalies obtained from EGM2008 and from GOCE time-wise solutions [mGal]

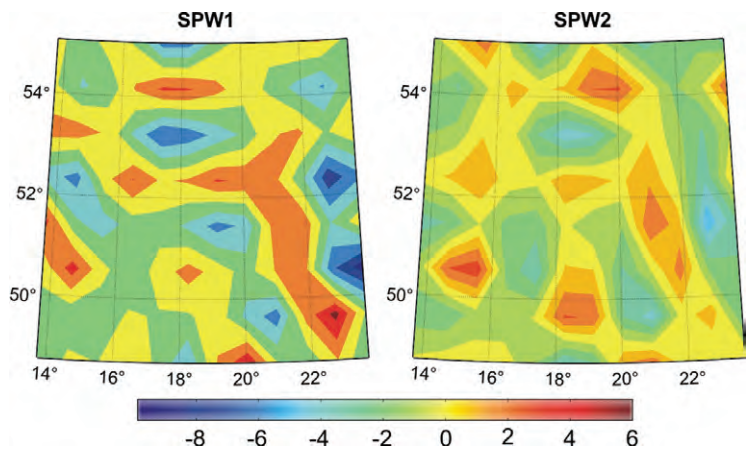


Fig. 3. Differences between free-air gravity anomalies obtained from EGM2008 and from GOCE space-wise solutions [mGal]



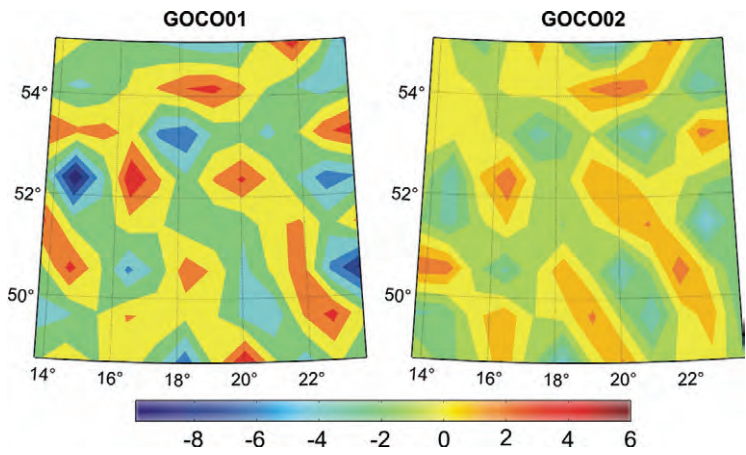


Fig. 4. Differences between free-air gravity anomalies obtained from EGM2008 and from GOCO models [mGal]

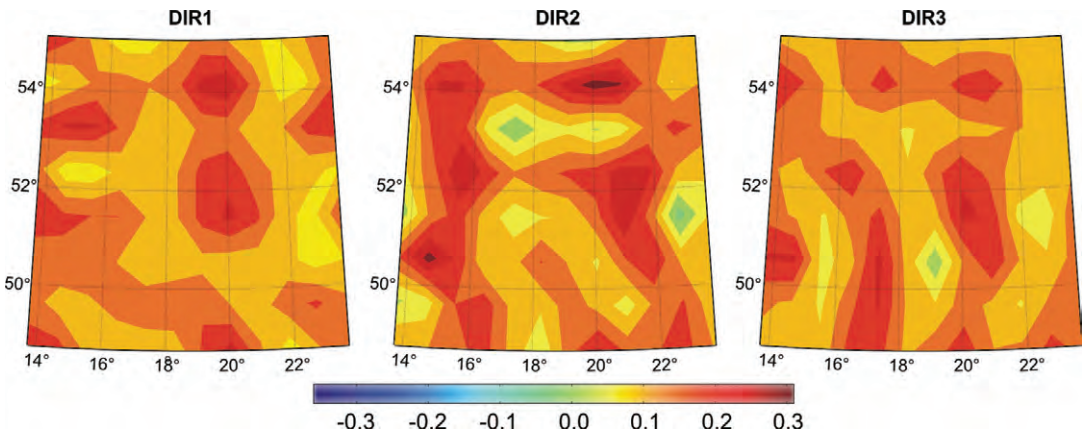


Fig. 5. Differences between height anomalies obtained from EGM2008 and from GOCE direct solutions [m]

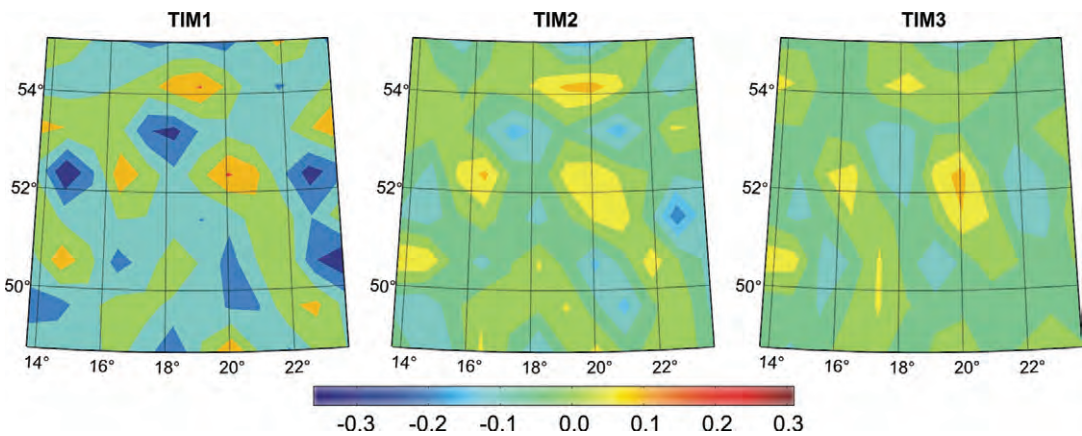


Fig. 6. Differences between height anomalies obtained from EGM2008 and from GOCE time-wise solutions [m]



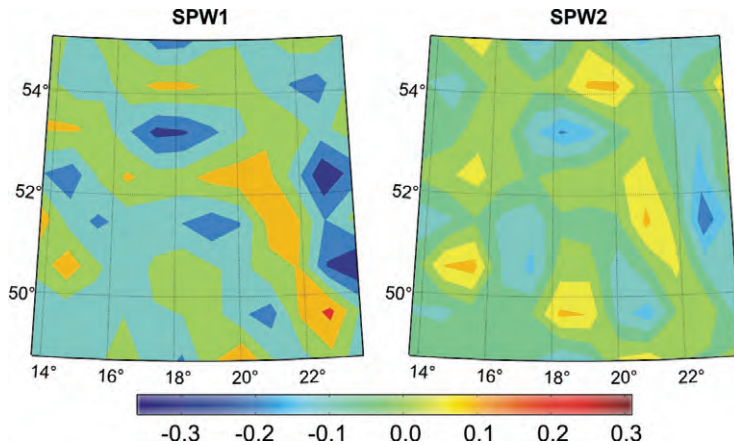


Fig. 7. Differences between height anomalies obtained from EGM2008 and from GOCE space-wise solutions [m]

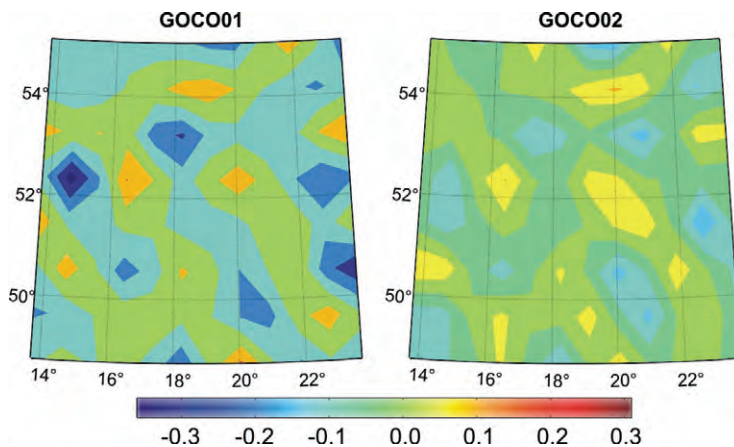


Fig. 8. Differences between height anomalies obtained from EGM2008 and from GOCO models [m]

The statistics of differences between GOCE-based GGMs and the EGM2008 in terms of height anomalies and gravity anomalies are given in Table 2. The results presented in Figures 1–4 and 5–8 together with those in Table 2 show clear improvement in terms of both height anomalies and gravity anomalies with growing data set in consecutive releases of GOCE solutions investigated. The improvement from 1<sup>st</sup> to 2<sup>nd</sup> release (except DIR1) is about 4 cm/1.3 mGal and from 2<sup>nd</sup> to 3<sup>rd</sup> release – about 2 cm/0.6 mGal. For TIM1, SPW1 and GOCO01 solutions the standard deviations are almost twice bigger than those for DIR1. This might be due to the DIR1 model was relied strongly on the a priori information from the EIGEN-5C geopotential model in the determination of the GOCE-

-based GGM. TIM3 has shown the best fit with the EGM2008 in both standard deviation and dispersion.

## 5. Comparison of GOCE-based gravity field models with GPS/levelling height anomalies

Height anomalies of 184 stations of high precision GPS/levelling control traverse across Poland (Fig. 9), of which 44 stations were considered as 1<sup>st</sup> order benchmarks and the remaining stations – as 2<sup>nd</sup> order benchmarks (difference in the length of GPS observing sessions and applied strategy of data processing) (Kryński, 2007b), were used to evaluate the GOCE--based GGMs.

Table 2. The statistics of differences between GOCE-based GGMs and the EGM2008 in terms of height anomalies and gravity anomalies ( $N_{\max} = 200$ )

GGM	Height anomalies [m]				Gravity anomalies [mGal]			
	Min	Max	Mean	STD	Min	Max	Mean	STD
DIR1	0.065	0.293	0.159	0.055	−2.986	3.195	−0.075	1.391
DIR2	−0.029	0.329	0.159	0.073	−5.343	4.420	−0.136	1.974
DIR3	0.011	0.268	0.159	0.050	−3.917	3.099	−0.053	1.329
TIM1	−0.312	0.213	−0.020	0.110	−8.679	6.280	−0.175	3.115
TIM2	−0.189	0.128	−0.011	0.064	−4.749	3.565	−0.149	1.774
TIM3	−0.111	0.122	−0.007	0.045	−2.814	3.029	−0.040	1.197
SPW1	−0.315	0.233	−0.009	0.107	−9.009	6.734	−0.159	3.020
SPW2	−0.193	0.122	−0.015	0.067	−4.845	3.719	−0.178	1.829
GOCO01	−0.352	0.216	−0.008	0.108	−9.875	6.194	−0.181	3.092
GOCO02	−0.156	0.110	−0.006	0.060	−4.130	3.109	−0.143	1.696

To provide a reliable comparison, data sets being compared should possibly represent the same spectral characteristics. Height anomalies of the GPS/levelling control traverse  $N_{GPS/levelling}$ , as obtained with the use of high resolution terrestrial gravity data, contain medium- and short-wave-length components. They were thus reduced to the spectral resolution of the GOCE model ( $N_{\max}^{GOCE} = 200$ ) by removing the medium-wavelength component

$$N_{EGM2008}^{N_{\max}=2160} - N_{EGM2008}^{N_{\max}=N_{\max}^{GOCE}+1} \quad (3)$$

using the EGM2008 as a reference model (Gruber, 2009). The difference  $\delta$  can be expressed as follows:

$$\delta = \left\{ N_{GPS/levelling} - N_{EGM2008}^{N_{\max}=2160} - N_{EGM2008}^{N_{\max}=N_{\max}^{GOCE}+1} \right\} - \{ N_{GOCE} + N_0 \} \quad (4)$$

with  $N_{GOCE}$  – the height anomaly determined using GOCE GGMs, and the additive constant  $N_0$  – a bias determined as follows (Heiskanen and Moritz, 1967):

$$N_0 = \frac{GM - GM_0}{R\bar{\gamma}} - \frac{W_0 - U_0}{\bar{\gamma}} \quad (5)$$

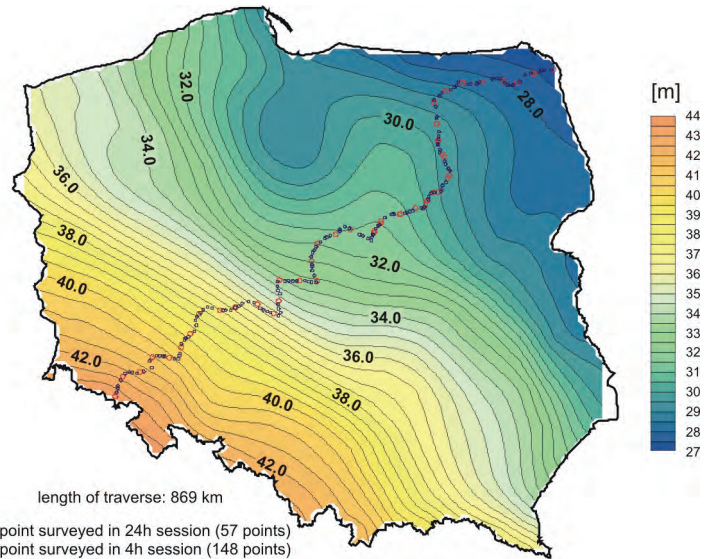


Fig. 9. GPS/levelling control traverse stations (Krynski, 2007b)

where  $M_0$  is the mass of the reference ellipsoid cor-

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Table 3. Statistics of the differences  $\delta$  between height anomalies obtained from GOCE-based GGMs and the respective ones from GPS/levelling along the control traverse [m]

GGM ( $N_{\max} = 200$ )	44 stations of 1 <sup>st</sup> order				184 stations of 1 <sup>st</sup> &2 <sup>nd</sup> order			
	Min	Max	Mean	STD	Min	Max	Mean	STD
DIR1	−0.099	0.231	0.064	0.087	−0.127	0.231	0.056	0.084
DIR2	−0.111	0.245	0.055	0.104	−0.132	0.245	0.043	0.103
DIR3	−0.103	0.248	0.066	0.107	−0.175	0.248	0.058	0.105
TIM1	−0.155	0.393	0.062	0.157	−0.175	0.393	0.049	0.157
TIM2	−0.159	0.261	0.037	0.109	−0.190	0.261	0.029	0.107
TIM3	−0.126	0.269	0.060	0.112	−0.164	0.269	0.055	0.108
SPW1	−0.125	0.360	0.079	0.135	−0.166	0.360	0.058	0.136
SPW2	−0.132	0.236	0.057	0.094	−0.143	0.236	0.046	0.092
GOCO01	−0.161	0.326	0.049	0.140	−0.190	0.326	0.041	0.139
GOCO02	−0.148	0.224	0.035	0.102	−0.184	0.224	0.030	0.099

It should be noted that the distribution of both differences  $\delta'$  and  $\delta$  along the control traverse exhibit a distinct periodicity. Similar behaviour to the one of DIR solution in Figure 10 has been observed for all other GOCE-based GGMs, i.e. TIM, SPW, and GOCO. Also the comparison of GOCE-derived height anomalies at the traverse sites with the corresponding ones obtained from the EGM2008 exhibits similar periodic pattern. Figure 11 shows the distribution (along the traverse's chord) of the differences between height anomalies obtained from DIR1 solution and the respective ones from the

EGM2008, truncated EGM2008 ( $N_{\max} = 200$ ), unfiltered, and filtered GPS/levelling height anomalies.

Consistency of spectral features of EGM2008 with GPS/levelling data as well as truncated EGM2008 with filtered GPS/levelling data is clearly seen in Figure 11.

The wavelengths of the observed variations of height anomaly differences have been estimated with the use of the least squares method by approximating them with the sine function

$$f(x) = A \cdot \sin(\omega \cdot x + \varphi) + D \quad (7)$$

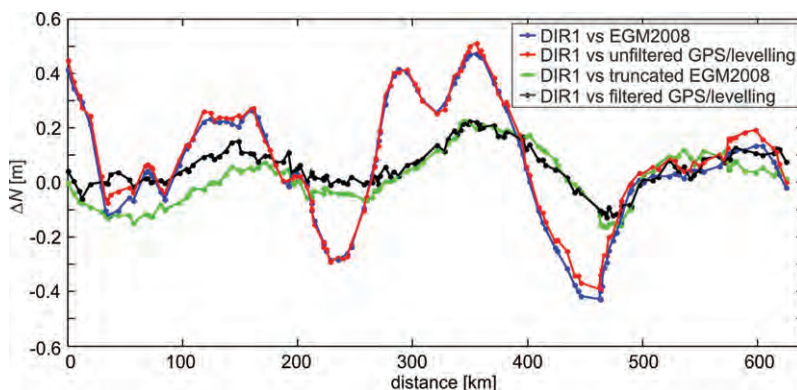


Fig. 11. Differences between height anomalies from DIR1 solution and the respective ones from the EGM2008 (blue), truncated EGM2008 (green), unfiltered GPS/levelling height anomalies (red), and filtered GPS/levelling height anomalies (black)

where  $A$  – the amplitude,  $\omega$  – the frequency,  $\varphi$  – the phase, and  $D$  – bias, are the parameters to be determined.

The approximation was performed along the traverse's chord and along the parallel, after applying appropriate projection to the actual distance along the traverse. The projection was used to determine the wavelength referred to geographic grid. The values of the determined wavelengths are given in Table 4. Figure 12 shows this pattern along the traverse's chord for the case of direct solutions.

The wavelengths shown in Table 4 reflect actual spatial resolution of the GOCE-based GGMs over Poland. Both, Figure 12 and Table 4 show that the wavelengths distinctly decrease from 1<sup>st</sup> to 2<sup>nd</sup> release for all four GOCE-based solutions investigated. It corresponds to the growth of spatial resolution of GGMs of consecutive releases which could be expected due to substantial extension of the length of observation period. No such progress is observed from 2<sup>nd</sup> to 3<sup>rd</sup> release. On the other hand, the amplitudes and phases of the periodic pattern in Figure 12 are similar in all four GOCE-based GGMs solutions. It indicates the consistency of those solutions with respect to high quality of GPS/levelling data at the control traverse. In addition, the fitting of the sine function to the height

anomalies differences has shown that their periodic pattern became very clear with the increase of the time span of GOCE observations, such as in the 3<sup>rd</sup> release solutions.

## 6. Conclusions

Height anomalies and gravity anomalies obtained from the current ten GOCE-based GGMs were compared with the corresponding functionals obtained from the EGM2008 and with high precision GPS/levelling height anomalies over Poland.

The results of comparison of GOCE-based GGMs with EGM2008 have shown good agreement. Except the DIR1, all approaches provided quite similar results within the same release. The DIR1 solution has presented the best performance among all approaches of the first release. It should not be a surprise since the EIGEN-5C geopotential model has been used for the a priori information when generating the solution. The TIM3 solution exhibits the best fit with the EGM2008 in terms standard deviations of both, height anomalies and gravity anomalies. The comparison shows also substantial improvements with increasing of the period of GOCE observation used for the solutions.

The deviation of the GOCE-based GGMs height anomalies from the corresponding ones at GPS/le-

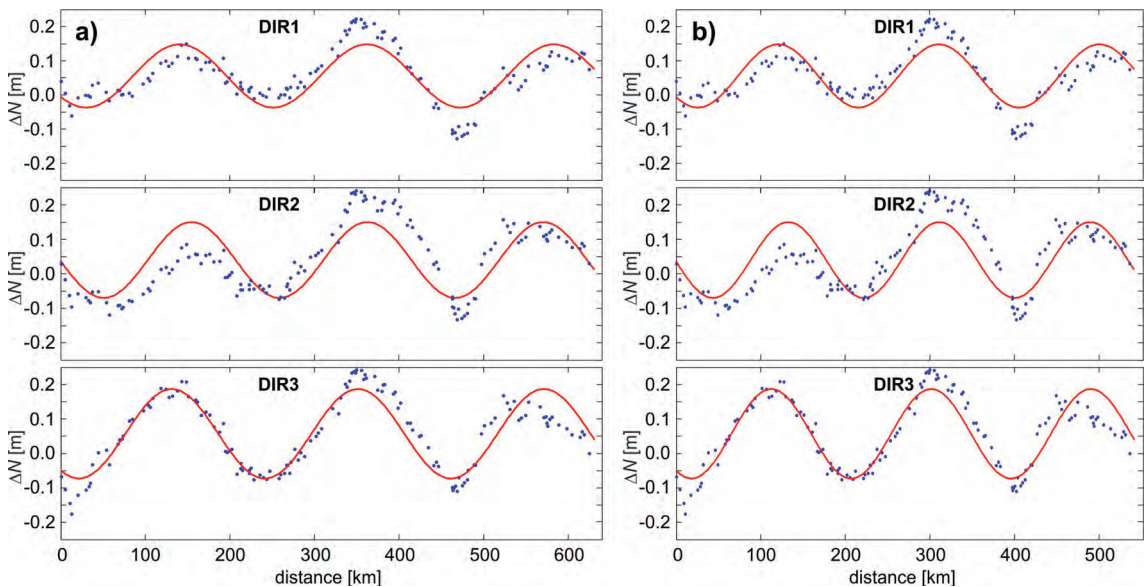


Fig. 12. Periodic pattern of the distribution of differences between the height anomalies from direct solutions GOCE GGMs and corresponding sites of GPS/levelling control traverse a) along the traverse's chord and b) along the parallel



Table 4. Estimated wavelengths of the differences between height anomalies from GOCE GGMs and corresponding sites of GPS/levelling control traverse along the traverse’s chord and along the parallel [km]

Model	Along the traverse’s chord			Along the parallel		
	1 <sup>st</sup> Release	2 <sup>nd</sup> Release	3 <sup>rd</sup> Release	1 <sup>st</sup> Release	2 <sup>nd</sup> Release	3 <sup>rd</sup> Release
DIR	221	208	220	184	173	183
TIM	225	221	227	187	183	188
SPW	250	203	–	207	169	–
GOCO	218	213	–	181	177	–

levelling control traverse sites is at the level of 10 cm. The investigation demonstrates that the differences of height anomalies along the control traverse exhibit a periodic pattern. The wavelengths of this pattern are within the range of 250–203 km along the traverse’s chord and 207–169 km after the projection into a parallel. An explicit improvement in terms of standard deviation with increasing of the time span of GOCE observations was detected from 1<sup>st</sup> to 2<sup>nd</sup> release. Also the wavelengths indicating spatial resolution of the model have decreased, as it could be expected. On the other hand, this improvement was not clear from 2<sup>nd</sup> to 3<sup>rd</sup> release. The results of the comparison of GOCE solutions with GPS/levelling data might be affected by residual medium- and short-wavelength components, still remained in the GPS/levelling data after filtering.

The results obtained indicate that the objectives of GOCE mission concerning the accuracy of 1–2 cm and 1 mGal with resolution ~100 km have not been reached yet. Further improvement should be expected with upcoming releases of GOCE-based GGMs.

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References

Bruinsma S.L., Marty J.C., Balmino G., Biancale R., Foerste C., Abrikosov O., Neumayer H., (2010): *GOCE Gravity Field Recovery by Means of the*

*Direct Numerical Method*, Proc. ESA Living Planet Symp., 28 June – 2 July 2010, Bergen, Norway, see also: [earth.esa.int/GOCE](http://earth.esa.int/GOCE).  
Drinkwater M., Floberghagen R., Haagsmans R., Muzi D., Popescu A., (2003): *GOCE: ESA’s first Earth Explorer core mission*, Space Science Reviews, Vol. 18, No 1–2, pp 419–432.  
ESA, (1999): *Report for mission selection of the four candidate Earth Explorer missions. Gravity Field and Steady-State Ocean Circulation Mission*, ESA SP-1233(1).  
Förste C., Flechtner F., Schmidt R., Stubenvoll R., Rothacher M., Kusche J., Neumayer K., Biancale R., Lemoine J., Barthelmes F., Bruinsma S., König R., Meyer U., (2008): *EIGEN-GL05C – A new global combined high-resolution GRACE-based gravity field model of the GFZ-GRGS cooperation*, EGU General Assembly 2008, Vienna, 13–18 April.  
Goiginger H., Hoeck E., Rieser D., Mayer-Guerr T., Maier A., Krauss S., Pail R., Fecher T., Gruber T., Brockmann J.M., Krasbutter I., Schuh W.-D., Jaeggi A., Prange L., Hausleitner W., Baur O., Kusche J., (2011): *The combined satellite-only global gravity field model GOCO02S*, EGU General Assembly 2011, Vienna, Austria, 4–8 April.  
Gruber T., (2009): *Evaluation of the EGM2008 gravity field by means of GPS-Leveling and sea surface topography solutions*, Special Issue: In: External quality evaluation reports of EGM2008, Newton’s Bulletin, Vol. 4, pp. 3–17.  
Heiskanen W.A., Moritz H., (1967): *Physical geodesy*, Freeman, San Francisco, London.  
Janák J., Pitoňák M., (2011): *Comparison and testing of GOCE global gravity models in Central Europe*, Journal of Geodetic Science, Vol. 1, No 4, pp. 333–347.



- Krynski J., (2007a): *Precise quasigeoid modelling in Poland – results and accuracy estimation* (in Polish), Monographic series of the Institute of Geodesy and Cartography, No 13, Warsaw (266 pp).
- Krynski J., (eds.) (2007b): *Polish National Report on Geodesy 2003 – 2006*, XXIV IUGG General Assembly, Perugia, Italy, 2–13 July 2007.
- Krynski J., Kloch G., (2009): *Evaluation of the performance of the new EGM08 global geopotential model over Poland*, Geoinformation Issues, Vol. 1, No 1, pp. 7–17.
- Krynski J., Lyszkowicz A., (2006): *The overview of precise quasigeoid modelling in Poland*, 2<sup>nd</sup> Workshop on Intern. Grav. Field Research 2006, 8–9 May 2006, Smolenice, Slovakia, Contributions to Geophysics and Geodesy, Special issue, WIGFR 2006, Geophysical Institute of Slovak Academy of Sciences, pp. 113–149.
- Krynski J., Lyszkowicz A., (2007): *Centimetre quasigeoid modelling in Poland using heterogeneous data*, IAG Proc. 1<sup>st</sup> Intern. Symp. of the Intern. Grav. Field Service (IGFS) “Gravity Field of the Earth”, 28 August – 1 September 2006, Istanbul, Turkey, pp. 37–42.
- Lyszkowicz A., (2009): *Assessment of accuracy of EGM08 model over the area of Poland*, Technical Sciences 12, UWM Olsztyn, DOI 10.2478/v10022-009-0011-x.
- Mayer-Gürr T., Kurtenbach E., Eicker A., (2010): *ITG-GRACE2010 Gravity Field Model*, <http://www.igg.uni-bonn.de/apmg/index.php?id=itg-grace2010>.
- McCarthy D., Petit G., (eds.) (2004): *IERS Conventions (2003)*, IERS Technical Note 32, BKG, Frankfurt.
- Migliaccio F., Reguzzoni M., Gatti A., Sanso F., Herceg M. (2011): *A GOCE-only global gravity field model by the space-wise approach*, Proc. 4<sup>th</sup> Intern. GOCE User Workshop, 31 March – 1 April 2011, Munich, ESA SP-696.
- Migliaccio F., Reguzzoni M., Sanso F., Tscherning C.C., Veicherts M., (2010): *GOCE data analysis: the space-wise approach and the first space-wise gravity field model*, Proc. ESA Living Planet Symp., 28 June – 2 July 2010, Bergen, Norway, ESA SP-686.
- Moritz H., (1980): *Geodetic Reference System 1980*, Bulletin Géodésique, Vol. 54, No 3, pp 395–405.
- Pail R., Bruinsma S., Migliaccio F., Förste C., Goiginger H., Schuh W., Höck E., Reguzzoni M., Brockmann J., Abrikosov O., Veicherts M., Fecher T., Mayrhofer R., Krasbutter I., Sansò F., Tscherning C.C., (2011): *First GOCE gravity field models derived by three different approaches*, Journal of Geodesy, Vol. 85, No 11, pp. 819–843.
- Pail R., Goiginger H., Mayrhofer R., Schuh W.-D., Brockmann J.M., Krasbutter I., Höck E., Fecher T., (2010a): *Global gravity field model derived from orbit and gradiometry data applying the time-wise method*, Proc. ESA Living Planet Symp., 28 June – 2 July 2010, Bergen, Norway, ESA SP-686.
- Pail R., Goiginger H., Schuh W.-D., Höck E., Brockmann J.M., Fecher T., Gruber T., Mayer-Gürr T., Kusche J., Jäggi A., Rieser D., (2010b): *Combined satellite gravity field model GOCO01S derived from GOCE and GRACE*, Geophys. Res. Lett., 37, L20314, doi:10.1029/2010GL044906.
- Pavlis N., Holmes S., Kenyon S., Factor J., (2008): *An Earth Gravitational Model to Degree 2160: EGM2008*, EGU General Assembly 2008, Vienna, 13–18 April.
- Rummel R., Gruber T., Koop R., (2004): *High level processing facility for GOCE: products and processing strategy*, Proc. 2<sup>nd</sup> Intern. GOCE User Workshop “GOCE, The Geoid and Oceanography”, Frascati, Italy, 8–10 March 2004, ESA SP-569.
- Šprlák M., Gerlach C., Omang O., Pettersen B., (2011): *Comparison of GOCE Derived Satellite Global Gravity Models with EGM2008, the OCTAS Geoid and Terrestrial Gravity Data: Case Study for Norway*, Proc. 4<sup>th</sup> Intern. GOCE User Workshop, TUM, Munich, Germany, 31 March – 1<sup>st</sup> April 2011, ESA SP-696.
- Torge W., (1991): *Geodesy*, 2<sup>nd</sup> edition, Walter de Gruyter, Berlin-New York.

# Ocena jakości na obszarze Polski modeli pola siły ciężkości opracowanych na podstawie danych z misji GOCE przy użyciu modelu EGM2008 i danych satelitarno-niwelacyjnych

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**Streszczenie.** Od połowy 2010 roku są udostępnione globalne modele geopotencjału opracowane na podstawie danych z misji GOCE. Pierwsze dwie generacje modeli geopotencjału z misji GOCE zawierały cztery różne rozwiązania podczas gdy trzecia – składała się zaledwie z dwóch rozwiązań. Jakość dostępnych modeli pola siły ciężkości z misji GOCE została w niniejszym opracowaniu oceniona w wyniku porównania obliczonych z nich anomalii wysokości i anomalii grawimetrycznych z odpowiednimi funkcjonalami obliczonymi z modelu geopotencjału EGM2008 oraz z anomaliami wysokości 184 stacji precyzyjnego satelitarno-niwelacyjnego trawersu kontrolnego.

Odchylenia standardowe różnic anomalii wysokości i anomalii grawimetrycznych pomiędzy uzyskanymi z opracowanych na podstawie danych z misji GOCE modeli geopotencjału i z modelu EGM2008 wynoszą odpowiednio 10 cm i 3 mGal. Dopasowanie modeli geopotencjału z misji GOCE do anomalii wysokości satelitarno-niwelacyjnego trawersu kontrolnego kształtuje się również na poziomie 10 cm. Uzyskane wyniki wskazują na poprawę w kolejnych generacjach modeli geopotencjału z misji GOCE.

**Słowa kluczowe:** model geopotencjału, GOCE, EGM2008, dane satelitarno-niwelacyjne, anomalia wysokości, anomalia grawimetryczna

